

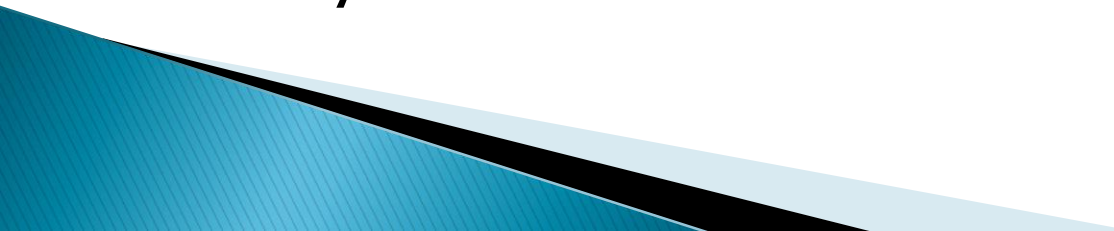
# What is an IMU?

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June 2015

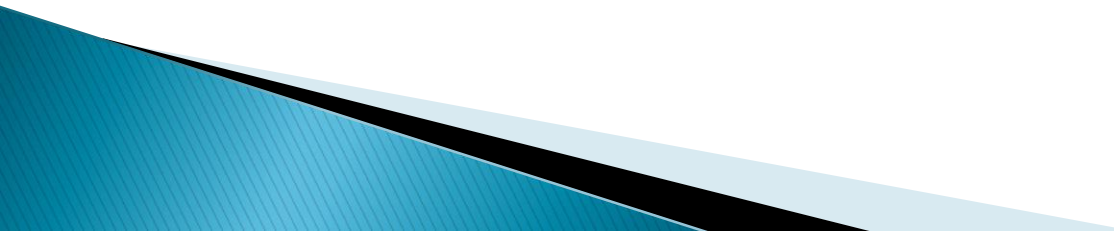
# Wikipedia says:

- ▶ An **inertial measurement unit (IMU)** is an electronic device that measures and reports a craft's velocity, orientation, and gravitational forces, using a combination of accelerometers and gyroscopes, sometimes also magnetometers.

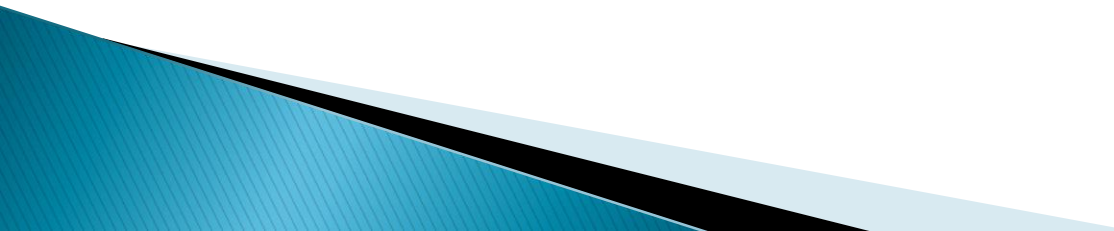
# Definitions

- ▶ Inertial: Pertaining to the physics that objects do not like to change orientation or speed.
  - ▶ Orientation: The pitch, bank, and heading of a body relative to a stationary reference like the Earth.
  - ▶ Velocity: Speed in a given direction.
  - ▶ Acceleration: How fast a body is changing its speed.
  - ▶ Accelerometer: A device that measures a body's acceleration.
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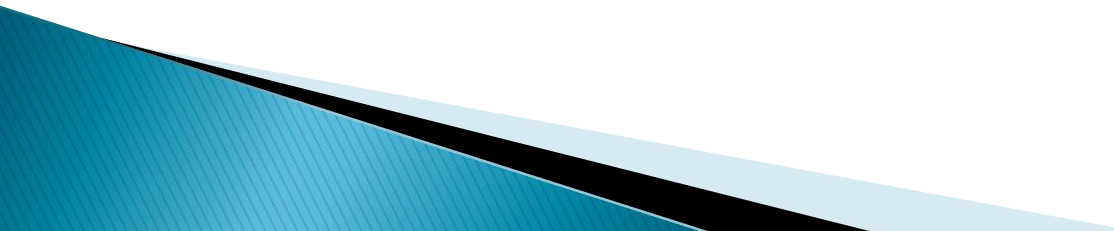
# Definitions

- ▶ Angular rate or rotational speed: How fast a body is spinning about itself. (RPM)
  - ▶ Gyroscope: A device that measures a body's angular rate.
  - ▶ Magnetometer: A device that measures the strength of a magnetic field. Often associated with the Earth's magnetic field.
  - ▶ Gravitational forces: How the body is subjected to accelerations.
- 

# Wikipedia says (again):

- ▶ An **inertial measurement unit (IMU)** is an electronic device that measures and reports a craft's velocity, orientation, and gravitational forces, using a combination of accelerometers and gyroscopes, sometimes also magnetometers.
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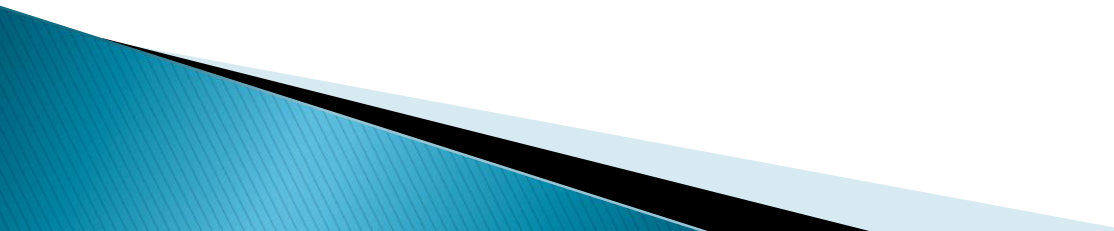
# But what is it really?

- ▶ **An inertial measurement unit (IMU)** is a device that tells you the following:
    - Pitch, roll, and heading
    - Speeds in your X, Y, and Z axis
    - Accelerations in your X, Y, and Z axis
    - Angular rates in your X, Y, and Z axis
    - Your location in the Earth's X, Y, and Z axis.
  - ▶ All this with only measuring physical values of accelerations and angular rates. No touch, vision, encoders, ...
  - ▶ Magnetometers and other sensors are 'cheating'.
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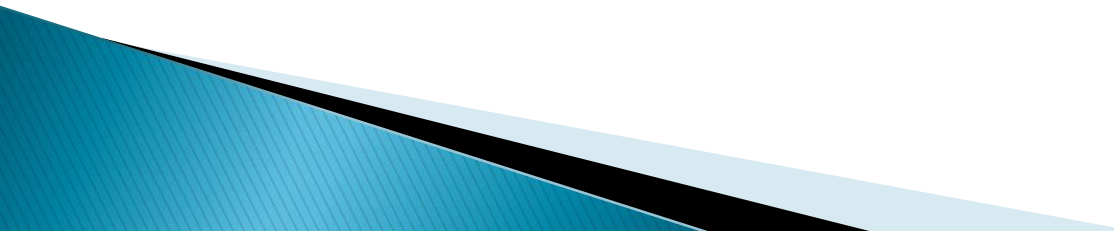
# Related Names

- ▶ **INS**      Inertial Navigation System
  - Full computer that uses an IMU and other sensors to navigate.
- ▶ **AHRS**      Attitude Heading Reference System
  - Just roll, pitch, and heading

# Examples

- ▶ Aircraft navigation system (INS)
  - ▶ Guidance system for a missile
  - ▶ Guidance system for a quadcopter
  - ▶ Navy ship destroyer navigation system
  - ▶ 3D mouse
- 

# Rainbow of IMUs

- ▶ 2D heading
  - ▶ 2D velocity
  - ▶ 2D orientation
  - ▶ 3D orientation (AHRS)
  - ▶ 3D orientation and velocities
  - ▶ 3D orientation, velocities, and location
  - ▶ Hybrids that merge in altimeter, magnetometer, and GPS data
- 

# Degrees of Freedom

- ▶ A 'Degree of Freedom' (DOF) is simply a way to count sensors that measure a unique parameter in a unique axis system.
- ▶ An (non enhanced) IMU is a 6 DOF device.
  - X, Y, and Z linear axis
  - P, Q, and R angular axis
- ▶ An IMU with magnetometer is 9 DOF
  - X, Y, and Z linear axis
  - P, Q, and R angular axis
  - P, Q, and R magnetometer axis

# Accelerometer (Linear)

- ▶ Determines the rate of change of a body's speed in a given direction. (m/s/s)
- ▶ Sensors leverage Newton's second law of motion
  - $F = m \cdot a$  or  $a = F / m$
  - Place a known mass on a spring. Measure the force on the spring then divide by the mass.
- ▶ Great video(s) to watch (The Engineer Guy)
  - <https://www.youtube.com/watch?t=245&v=KZVgKu6v808>

# Gyroscope (angular rate)

- ▶ Spinning mass in gimbal
  - Heavy, large, suffers from 'Gimbal lock'
- ▶ Micro-Electro-Mechanical system (MEMS)
  - Tuning fork
  - Cheap
- ▶ Fiber Optic Gyro (FOG)
  - Change in how long it takes light to go around a coil of fiber.
  - \$\$\$
- ▶ Ring Laser Gyro (RLG)
  - Change in how long it takes light to go around a race track.
  - \$\$\$
- ▶ Resonant Sphere
  - Watch how a 'bell' rings.
  - \$\$\$

# Math principles

- ▶ Integration of measured values to yield desired results.
  - Integrate angular velocity into angular position
    - Roll, Pitch, Heading
  - Integrate linear acceleration into linear speed
    - X, Y, and Z speed
  - Integrate linear speed into linear position.
    - X, Y, and Z position

# Integration

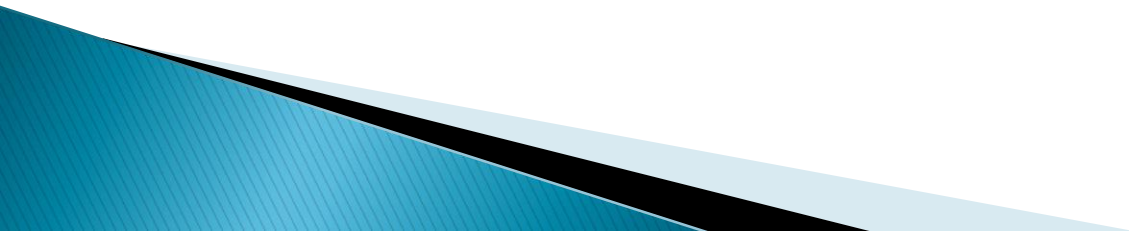
- ▶ “All” we need is to solve these equations:

- ▶  $\phi = \int_0^\infty \dot{\phi} dt$      $\theta = \int_0^\infty \dot{\theta} dt$      $\psi = \int_0^\infty \dot{\psi} dt$

- ▶  $\dot{x} = \int_0^\infty \ddot{x} dt$      $\dot{y} = \int_0^\infty \ddot{y} dt$      $\dot{z} = \int_0^\infty \ddot{z} dt$

- ▶  $x = \int_0^\infty \dot{x} dt$      $y = \int_0^\infty \dot{y} dt$      $z = \int_0^\infty \dot{z} dt$

# WRONG!



# Numerical integration

- ▶ Rather than symbolic integration, we use numerical integration.
  - No college course needed.
  - Pretty easy to understand.

# An example

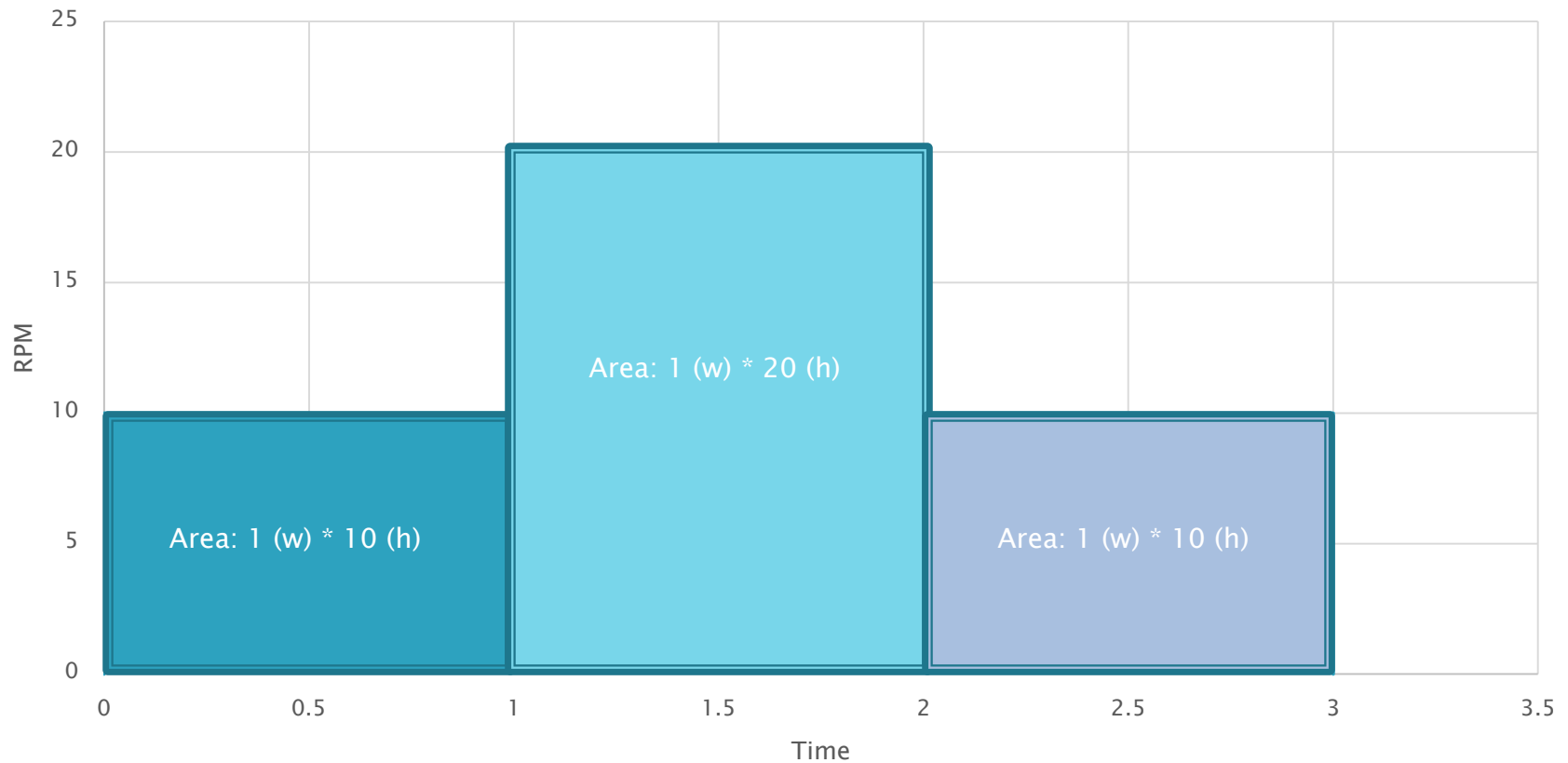
- ▶ You are in a car traveling west.
- ▶ For the first hour you are going 10 MPH
- ▶ The second hour you are going 20 MPH
- ▶ The third hour you are going 10 MPH
  
- ▶ How far did you travel after the first hour?
  - $1\text{H} * 10\text{ MPH} = 10\text{ miles}$
- ▶ How far did you travel after the second hour?
  - $(1\text{H} * 10\text{ MPH}) + 1\text{H} * 20\text{ MPH} = 30\text{ miles}$
- ▶ How far did you travel after the third hour?
  - $(1\text{H} * 10\text{ MPH} + 1\text{H} * 20\text{ MPH}) + 1\text{H} * 10\text{ MPH} = 40\text{ miles}$

# Continued

- ▶ You are spinning on a merry-go-round.
- ▶ For the first minute you are going 10 RPM
- ▶ The second minute you are going 20 RPM
- ▶ The third minute you are going 10 RPM
  
- ▶ How far did you rotate after the third minute?
  - $1\text{M} * 10\text{ RPM} + 1\text{M} * 20\text{ RPM} + 1\text{M} * 10\text{ RPM}$
  - Or 40 revolutions

# A graphical approach

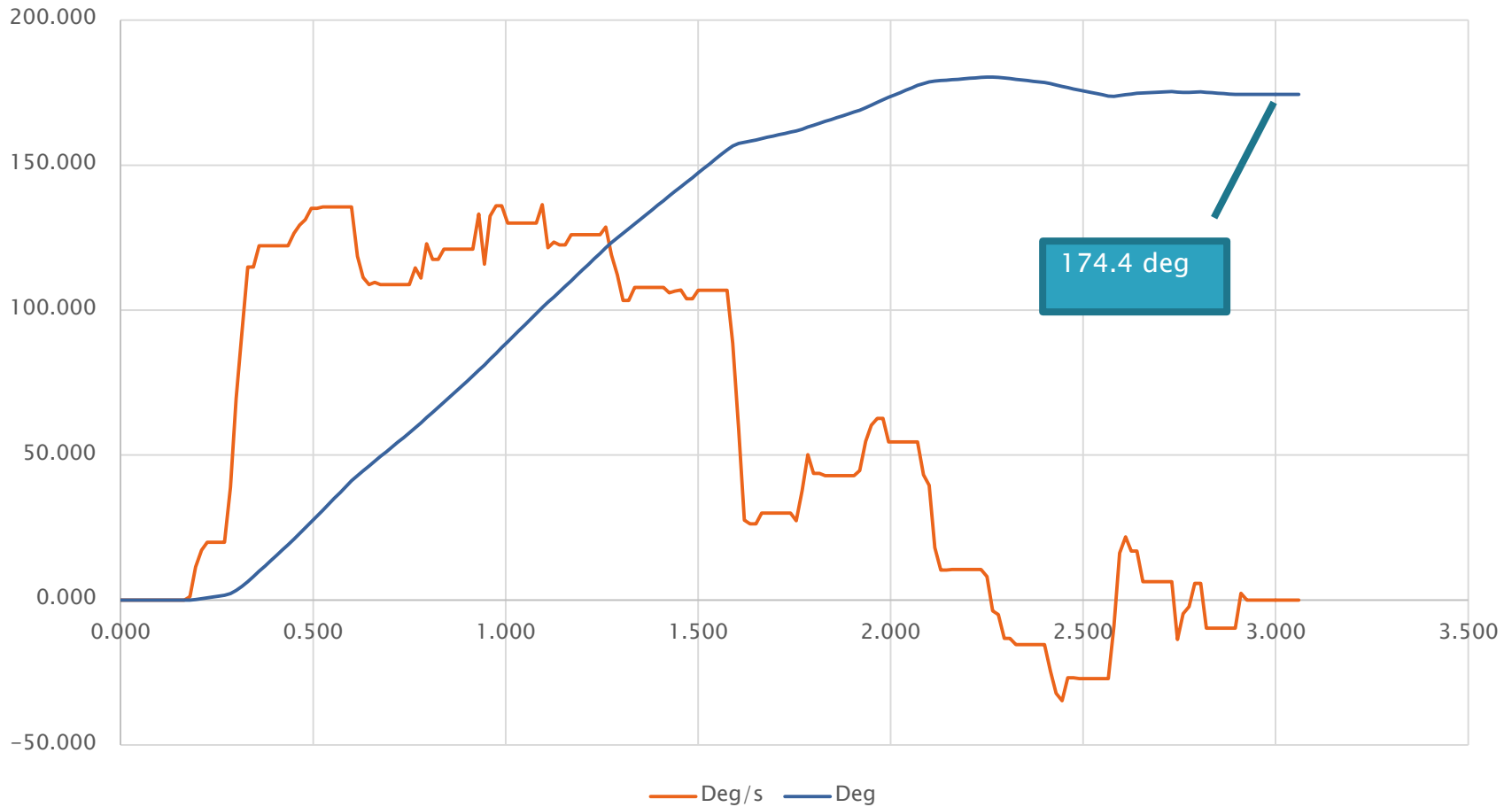
Example



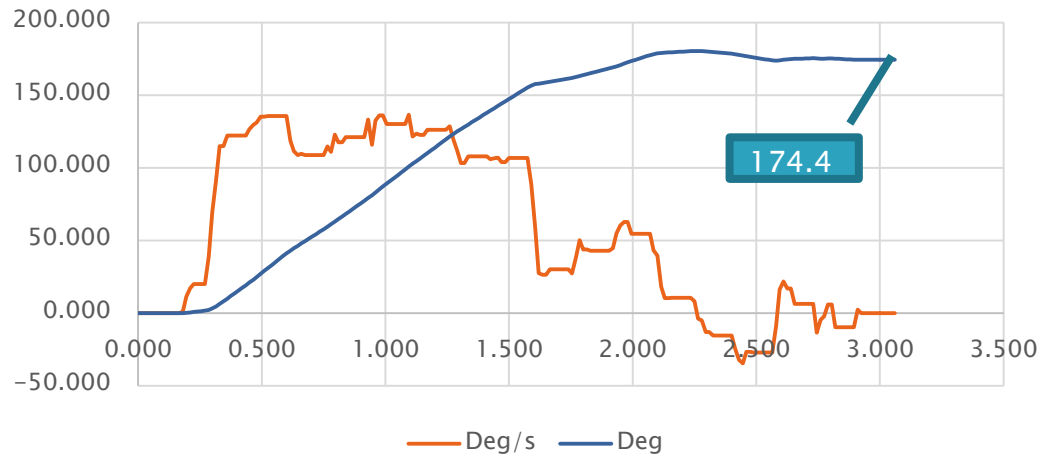
# Basic Implementation

- ▶  $\text{Roll} = \text{Roll} + \text{RollRate} * \text{timeInc};$
- ▶  $\text{Pitch} = \text{Pitch} + \text{PitchRate} * \text{timeInc};$
- ▶  $\text{Heading} = \text{Heading} + \text{PitchRate} * \text{timeInc};$
  
- ▶  $\text{xSpeed} = \text{xSpeed} + \text{xAccel} * \text{timeInc};$
- ▶ ...
- ▶  $\text{xPosition} = \text{xPosition} + \text{xSpeed} * \text{timeInc};$
- ▶ ...

# Real Data for a 180 turn



# Something to Notice

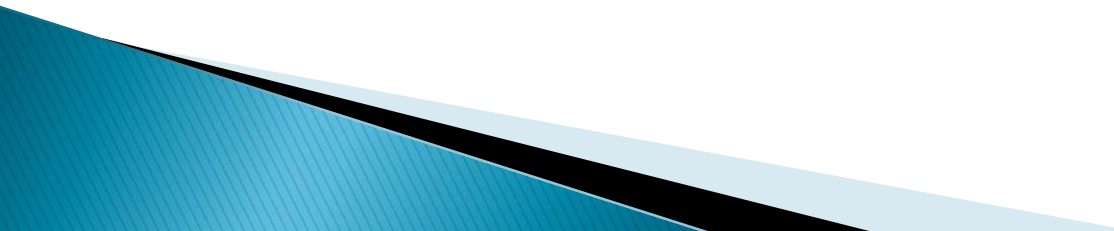


What happened to the 5.6 degrees?

# Sensor Specs

- ▶ Accuracy (how right the answer is)
  - The less the accuracy depends on temperature, magnetic fields, vibration, ... the better.
- ▶ Precision (how many decimal points you get)
  - The more precise the better.
  - All sensors are analog at the start. Unless you are using an analog computer, the analog value must get converted to a number at some point. The better the converter the better your results.
- ▶ Range
  - Best to just cover the rates and accelerations you need. A  $\pm 100$  g accelerometer on an indoor robot robs you of precision. A  $\pm 1$  g accelerometer on a rocket will saturate.
- ▶ Random errors
  - Due mostly to noise in the sensor.

# Sample/Integration Rate

- ▶ How often you sample
  - ▶ The faster you sample the finer detail you can account for.
  - ▶ The faster you sample, the more computation power you need.
  - ▶ I have used systems that operate from as low as 10 to as much as 10,000 times a second.
- 

# Calibration

## ▶ Scale factor

- Datasheet may say full scale is 100 degrees/second but in fact it is 98.7.

## ▶ Offset

- When the unit is still, the voltage is rarely 0.0 or the count 0.

## ▶ Solution

- $\text{realValue} = (\text{rawSensor} - \text{offset}) * \text{scaleFactor};$
- Offset can be determined by reading the “at rest” value.
- Scale factor is more difficult...

# Scale Factor

## ▶ Accelerometer

- At rest, the vertical (z) axis will experience  $9.8\text{m/s/s}$  (1g) due to gravity.
- Record the raw value then invert the sensor.
- Now the sensor is under 1g the other way.
- Record this raw value.
- The difference in raw values is equal to 2 g's of acceleration.

## ▶ Gyro

- Need a rate table. Repurpose an old phonograph! You can get 33.3 and 45 RPM from one!

# Temperature Effects

- ▶ MEMS sensors are fairly sensitive to temp
  - Calibrate at different temperatures
  - Or
  - Maintain the device at a constant temperature
    - Heater inside a temp controlled oven

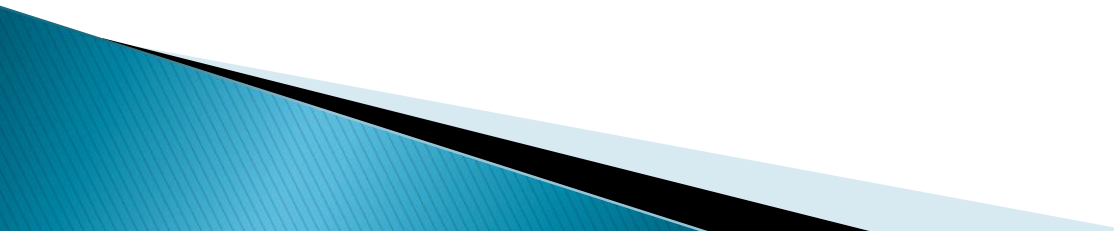
# Absolute vs Relative

- ▶ A strict IMU (nothing but inertial sensors) is for the most part a relative sensor.
- ▶ It can only tell you how far you have turned or moved from when it was first turned on.
  - It can only tell that you are now 40 revolutions from the start, not that you are now heading at  $43.2^\circ$
- ▶ The exception is pitch and roll.

# Enhanced IMUs

- ▶ IMUs that add other sensors such as
  - Magnetometers
  - GPS
  - Barometers
  - RADAR / LIDAR
  - Radio altimeters
  - ...
- ▶ Enhanced IMUs can now give absolute answers to some parameters.

# If you have a GPS why use an IMU at all?

- ▶ GPS does not give you pitch and roll.
  - ▶ The accuracy of GPS is great long term, but not so good short term.
  - ▶ The accuracy of an IMU is great short term, but terrible long term.
  - ▶ Merge the two and you get the both of best worlds!
    - Kalman filter (KF)
    - Enhanced Kalman filter (EKF)
    - Complimentary filter
- 

# Magnetometers

- ▶ Magnetometers are often used in enhanced IMUs.
- ▶ By measuring the Earth's magnetic field you can determine your absolute heading.
- ▶ But...
  - Heading is relative to magnetic north not true.
  - Calibration is somewhat complex.
  - Very sensitive to:
    - Ferrous metals
    - Magnetic fields such as drive and servo motors
    - Magnetic fields such as created by electric circuits.

# What can I expect?

- ▶ If you have
  - MEMS type sensors
  - 100 Hz integration rate
  - Fully calibrated
  - Minimal vibration
  - Under 1 g accelerations
  - Under 200 deg/sec turn rates
    - In angular space **at best** 15 deg/hour
    - In linear space about %5 percent/hour
- ▶ All errors grow in time.
  - Position is the worst due to double integration.

# What can I expect?

- ▶ Invest \$100,000
  - FOG or RLG
  - Vibration damped
  - Top of line accelerometers
  - High computation power
    - 1 degree per hour
    - 0.1% per hour linear

# Ready to go IMUs

- ▶ UM7 (LT) (\$130 from Pololu)
  - 9 DOF (acc, gyro, mag)
  - GPS support
  - EKF
  - Unknown sensor supplier
- ▶ BNO055 (\$35 from AdaFruit)
  - 9 DOF
  - EKF
  - Bosh based

# Roll Your Own (Sparkfun)

- ▶ Various 6 axis MEMS devices
  - InvenSense and ST based
- ▶ Various 9 axis MEMS devices
  - InvenSense and ST based
- ▶ DIYDrones ArduIMU (IMU + GPS)
- ▶ Buying guide:
  - [https://www.sparkfun.com/pages/accel\\_gyro\\_guide](https://www.sparkfun.com/pages/accel_gyro_guide)

# Roll Your Own (AdaFruit)

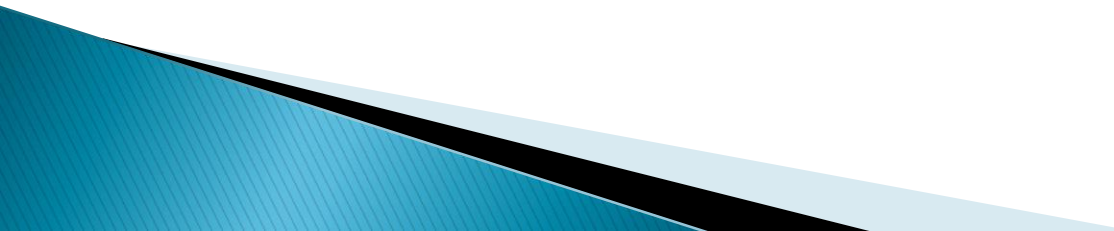
- 9 DOF (\$20)
  - ST based
- 10 DOF (\$25)
  - ST based

# Roll Your Own (Pololu)

## ► Pololu

- Mini IMU (\$20)
  - 9 DOF based on ST parts
- Alt IMU (\$22)
  - 10 DOF based on ST parts
- 3 DOF accel
- 3 DOF gyro
- 3 DOF mag

# Sensor Manufacturers

- ▶ Hobbyist tier
    - ST
    - Invensense
    - Analog Devices
  - ▶ Pro tier
    - Sensoror
    - Murata
    - Moog–Crossbow
    - KVH
    - Various defense contractors
- 

# Questions?

